

$a > 0, a \neq 4, \frac{x^2}{a^2} + \frac{y^2}{a^2 - 16} = 1$

: ( )

$a, a^2 \neq a^2 - 16$  (1)

$a < -4, a > 4, a^2 - 16 > 0$  (2)

$a > 4$  (2),  $a > 0, a \neq 4$

$a > 4$ :

$(a > 4, \frac{x^2}{a^2} + \frac{y^2}{a^2 - 16} = 1$

$A(0, -\sqrt{a^2 - 16}), y$

$F_1(4, 0), c^2 = a^2 - (a^2 - 16) = 16, F_1(c, 0)$

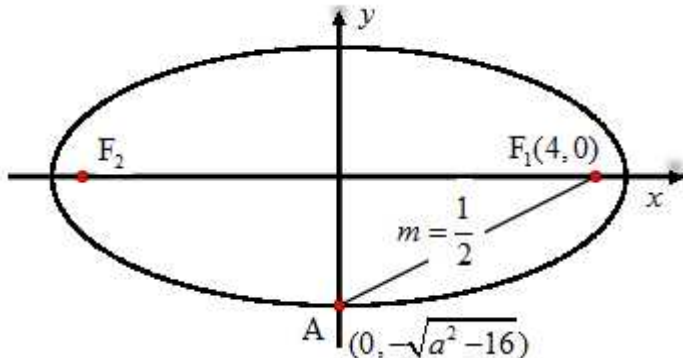
$m_{AF_1} = \tan 26.566^\circ = \frac{1}{2}$ ,  $x$   $26.566^\circ$   $AF_1$

$\frac{1}{2} = \frac{-\sqrt{a^2 - 16} - 0}{0 - 4} \rightarrow \sqrt{a^2 - 16} = 2$

$a^2 - 16 = 4 \rightarrow a^2 = 20, \sqrt{-20 + 16} = 2 \rightarrow 2 = 2 \text{ o.k.}$

$\frac{x^2}{20} + \frac{y^2}{4} = 1, a^2 = 20$

$\frac{x^2}{20} + \frac{y^2}{4} = 1$

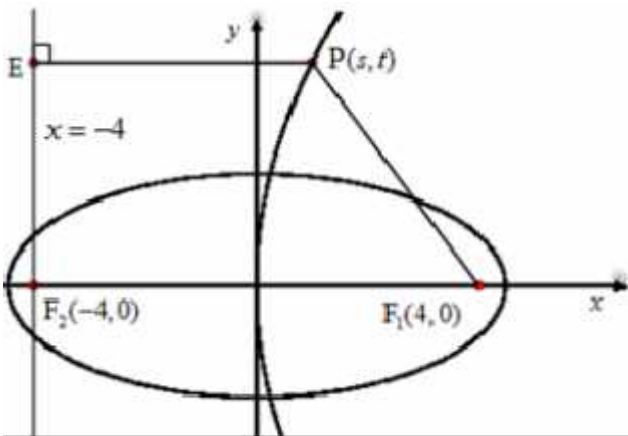


$(F_2(-4, 0)) x = -4, F_1(4, 0)$

$x = -4, F(4, 0)$

$y^2 = 16x, 8$

$PE = PF_1, P(s, t)$



$\sqrt{(s-4)^2 + (t-0)^2} = s - (-4)$

$(s-4)^2 + (t-0)^2 = (s+4)^2$

$s^2 - 8s + 16 + t^2 = s^2 + 8s + 16$

$t^2 = 16s \rightarrow y^2 = 16x$

$y^2 = 16x$

.BDC  $\overline{AF}$   $AF \perp f_{BDC}$  (1).

$$\boxed{\overline{AP} \cdot \overline{BD} = 0} \quad - \quad \overline{AP} \perp \overline{BD} \quad AF \quad P \quad :$$

.ABD  $\overline{CH}$   $CH \perp f_{ABD}$  (2)

$$\overline{CP} \cdot \overline{BD} = 0 \quad - \quad \overline{CP} \perp \overline{BD} \quad CH \quad P$$

$$\overline{AC} \cdot \overline{BD} = (\overline{AP} + \overline{PC}) \cdot \overline{BD}$$

$$\overline{AC} \cdot \overline{BD} = \overline{AP} \cdot \overline{BD} + \overline{PC} \cdot \overline{BD}$$

$$\overline{AC} \cdot \overline{BD} = 0 + 0 = 0 \rightarrow \boxed{\overline{AC} \perp \overline{BD}}$$

$$\overline{AH} \cdot \overline{BD} = 0 \quad , \overline{AH} \perp \overline{BD}$$

$$\overline{AH} \cdot \overline{BD} = (\overline{AC} + \overline{CH}) \cdot \overline{BD}$$

$$\overline{AH} \cdot \overline{BD} = \overline{AC} \cdot \overline{BD} + \overline{CH} \cdot \overline{BD}$$

$$\overline{AH} \cdot \overline{BD} = 0 + 0 = 0 \rightarrow \boxed{\overline{AH} \perp \overline{BD}}$$

.  $\cos \sphericalangle CBD = \cos \sphericalangle ABD$

,  $\sphericalangle CBD = \sphericalangle ABD$   $AB = BC$

$$\boxed{\overline{BD} = u} \quad \boxed{\overline{BC} = v} \quad \boxed{\overline{BA} = w}$$

$$AB = BC \rightarrow |w| = |v|$$

$$\cos \sphericalangle CBD = \cos \sphericalangle ABD$$

$$\Leftrightarrow \frac{\overline{BC} \cdot \overline{BD}}{|\overline{BC}| |\overline{BD}|} = \frac{\overline{BA} \cdot \overline{BD}}{|\overline{BA}| |\overline{BD}|}$$

$$\Leftrightarrow \frac{\overline{BC} \cdot \overline{BD}}{|v|} = \frac{\overline{BA} \cdot \overline{BD}}{|w|}$$

$$\Leftrightarrow \overline{BC} \cdot \overline{BD} = \overline{BA} \cdot \overline{BD}$$

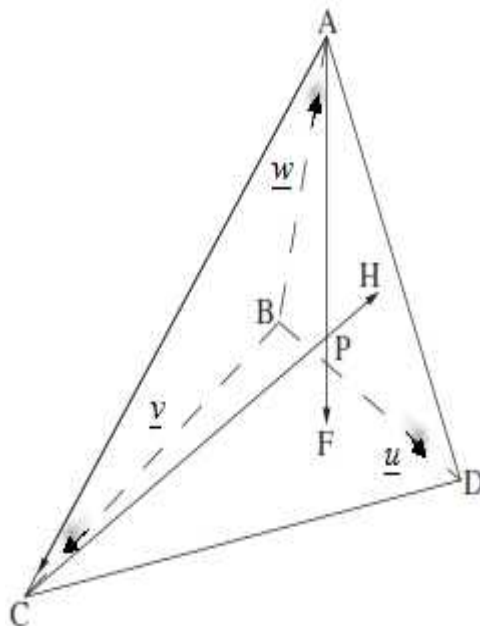
$$\Leftrightarrow \overline{BC} \cdot \overline{BD} - \overline{BA} \cdot \overline{BD} = 0$$

$$\Leftrightarrow \overline{BD} \cdot (\overline{BC} - \overline{BA}) = 0$$

$$\Leftrightarrow \overline{BD} \cdot (\overline{BC} + \overline{AB}) = 0$$

$$\Leftrightarrow \overline{BD} \cdot (\overline{AB} + \overline{BC}) = 0$$

$$\Leftrightarrow \overline{BD} \cdot \overline{AC} = 0 \quad true \leftarrow \overline{AC} \perp \overline{BD}$$



$\cdot z = 1 \text{ cis } \Gamma \quad , z = \cos \Gamma + i \sin \Gamma \cdot$

$\cdot w = r \text{ cis } S \quad , |w| = r \quad (r > 0)$

$\cdot 0^\circ < \Gamma, S < 90^\circ \quad , 0^\circ < \arg(z), \arg(w) < 90^\circ \quad , \quad z, w$

$z = \frac{w}{\bar{w}}$

$z = \frac{r \text{ cis } S}{r \text{ cis } (-S)} = \text{cis } 2S$

$\cdot ( \quad ) \Gamma = 2S \quad - \quad , 0^\circ < \Gamma, S < 90^\circ \quad - \quad , \text{cis } \Gamma = \text{cis } 2S \quad :$

$\cdot 0^\circ < S < 45^\circ \quad - \quad , 0^\circ < \Gamma < 90^\circ \quad -$

$w = r \text{ cis } S \quad \rightarrow \quad \boxed{w = r \text{ cis } \frac{\Gamma}{2}}$

$\boxed{\bar{w} = r \text{ cis } (-\frac{\Gamma}{2})}$

$\frac{1}{w} = \frac{\text{cis } 0^\circ}{r \text{ cis } \frac{\Gamma}{2}} \quad \rightarrow \quad \boxed{\frac{1}{w} = \frac{1}{r} \text{ cis } (-\frac{\Gamma}{2})}$

$\cdot \frac{1}{w} = \frac{1}{r} \text{ cis } (-\frac{\Gamma}{2}) \quad , \quad \bar{w} = r \text{ cis } (-\frac{\Gamma}{2}) \quad , \quad w = r \text{ cis } \frac{\Gamma}{2} \quad :$

$\cdot ( \quad , z = 1 \text{ cis } \Gamma$

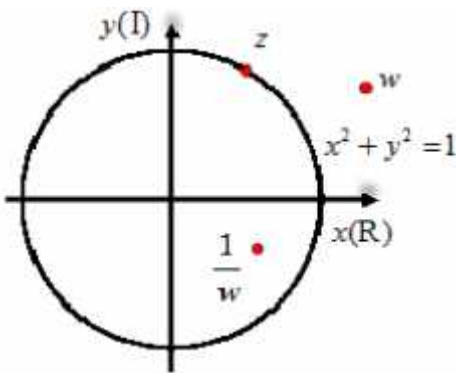
$) \frac{1}{w} = \frac{1}{r} \text{ cis } (-\frac{\Gamma}{2}) \quad w = r \text{ cis } \frac{\Gamma}{2} \quad ,$

$\cdot 0^\circ < \frac{\Gamma}{2} < 45^\circ \quad ,$

$w = r \text{ cis } \frac{\Gamma}{2} \quad : r > 1$

$\cdot -45^\circ < -\frac{\Gamma}{2} < 0^\circ \quad , \frac{1}{r} < 1$

$\frac{1}{w} = \frac{1}{r} \text{ cis } (-\frac{\Gamma}{2})$



$\cdot a_2 = z = \text{cis } \Gamma \quad - \quad a_1 = \frac{1}{w} = \frac{1}{r} \text{ cis } (-\frac{\Gamma}{2}) \quad a_n \cdot$

$\cdot q = \frac{a_2}{a_1} = \frac{z}{1/w} = zw = \text{cis } \Gamma \cdot r \text{ cis } \frac{\Gamma}{2} = r \text{ cis } 1.5\Gamma$

$\cdot ( \quad - \quad ) a_3 = a_2 q^2 = \text{cis } \Gamma \cdot (r \text{ cis } 1.5\Gamma)^2 = \text{cis } \Gamma \cdot r^2 \cdot \text{cis } 3\Gamma = \boxed{r^2 \text{ cis } 4\Gamma}$

$\cdot a_5 = r^3 \text{ cis } 5.5\Gamma \quad :$

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$$f(x) = \sqrt{2x-1} \cdot e^{x^2-x}$$

$$\boxed{x \geq 0.5}$$

$$2x-1 \geq 0$$

$$x \geq 0.5$$

$$f'(x) = \frac{2}{2\sqrt{2x-1}} \cdot e^{x^2-x} + \sqrt{2x-1} \cdot (2x-1) \cdot e^{x^2-x}$$

$$x > 0.5$$

$$, x = 0.5$$

$$, x > 0.5 \quad f'(x) > 0$$

$$x = 1$$

(1)

$$(1,1)$$

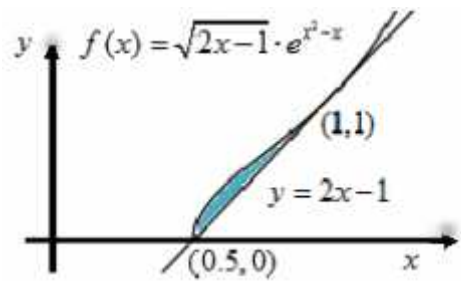
$$, f(1) = \sqrt{2 \cdot 1 - 1} \cdot e^{1^2-1} = 1$$

.2

$$, f'(1) = \frac{2}{2\sqrt{2 \cdot 1 - 1}} \cdot e^{1^2-1} + \sqrt{2 \cdot 1 - 1} \cdot (2 \cdot 1 - 1) \cdot e^{1^2-1} = 1 + 1 = 2$$

$$y - 1 = 2(x - 1) \rightarrow \boxed{y = 2x - 1}$$

$$y = 2x - 1$$



$f(x)$

$x -$

$(0.5, 0)$

" "

(2)

$x -$

( )

(3)

$$V = f \int_{0.5}^1 (\sqrt{2x-1} \cdot e^{x^2-x})^2 dx - f \int_{0.5}^1 (2x-1)^2 dx$$

$$V = f \int_{0.5}^1 ((2x-1) \cdot e^{2x^2-2x} - (2x-1)^2) dx$$

$$V = f \int_{0.5}^1 \left( \frac{1}{2} \cdot e^{2x^2-2x} (4x-2) - (2x-1)^2 \right) dx$$

$$V = f \left( \frac{1}{2} \cdot e^{2x^2-2x} - \frac{(2x-1)^3}{2 \cdot 3} \right) \Big|_{0.5}^1$$

$$x=1: f \left( \frac{1}{2} - \frac{1}{6} \right) = \frac{1}{3} f$$

$$x=0.5: f \left( \frac{e^{-0.5}}{2} - 0 \right) = \frac{1}{2\sqrt{e}} f$$

$$\left. \begin{array}{l} x=1: f \left( \frac{1}{2} - \frac{1}{6} \right) = \frac{1}{3} f \\ x=0.5: f \left( \frac{e^{-0.5}}{2} - 0 \right) = \frac{1}{2\sqrt{e}} f \end{array} \right\} V = \left( \frac{1}{3} - \frac{1}{2\sqrt{e}} \right) f$$

"  $\left( \frac{1}{3} - \frac{1}{2\sqrt{e}} \right) f \approx 0.03f \approx 0.0945$  :

$-1.1 \leq x \leq 3.1$

$-1.1 \leq x < 0$      $2 < x \leq 3.1$  :     $0 < x < 2$  :    : I

( ) II

$f'(x)$  I ,  $f(x)$  II

$f(x)$  II :

$g(x) = \ln(f(x))$

$\ln(f(x))$  (1)

$-1.1 \leq x < -1$      $1 < x < 3$

$-1.1 \leq x < -1$      $1 < x < 3$      $g(x) = \ln(f(x))$  :

( ) ,  $x = -1$  -  $x = 1$  ,  $x = 3$  (2)

$\lim_{x \rightarrow 3^-} g(x) = \lim_{x \rightarrow 3^-} \ln(f(x)) = \lim_{x \rightarrow 3^-} \ln(0^+) = -\infty$

$\lim_{x \rightarrow 1^+} g(x) = \lim_{x \rightarrow 1^+} \ln(f(x)) = \lim_{x \rightarrow 1^+} \ln(0^+) = -\infty$

$\lim_{x \rightarrow -1^-} g(x) = \lim_{x \rightarrow -1^-} \ln(f(x)) = \lim_{x \rightarrow -1^-} \ln(0^+) = -\infty$

(5)

$g(x) \rightarrow -\infty$

$x = -1$  -  $x = 1$  ,  $x = 3$  :

$g(x) = \ln(f(x))$  (3)

$g'(x) = \frac{f'(x)}{f(x)}$

$x = 2$  ,  $g(x)$  ,  $x = 0$  , I ,  $f'(x)$

$x = 2$   $x = 2$

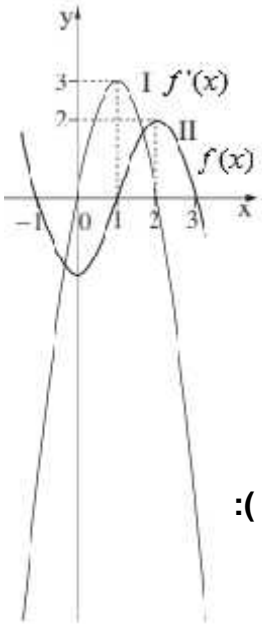
$g(2) = \ln(f(2)) = \ln 2$

$(2, \ln 2)$ , max :

$f'(x)$  ,  $g'(x)$  (4)

$g(x)$  ,  $-1.1 < x < -1$  ,  $2 < x < 3$  : ,  $1 < x < 2$  :

$-1.1 < x < -1$  ,  $2 < x < 3$  ,  $1 < x < 2$   $g(x)$  :



.( )  $f(x)$   $y=1$  (5)

.  $g(x) = \ln(f(x)) = \ln(1) = 0$  -  $f(x) = 1$

.( )  $x$  -  $g(x)$

.  $\ln(1.5) < g(-1.1) < \ln(2)$   $1.5 < f(-1.1) < 2$  :

