

(") () B - A - v -
 . 15+v - A B 15-v
 . () B t -
 :

s - "	v - "	t -	A -	
5v	v	5	A -	
5(15-v)	15-v	5	B -	
tv	v	t	B - A -	B
tv	15-v	$\frac{tv}{15-v}$	A - B -	
tv	15+v	$\frac{tv}{15+v}$	B - A -	

: , 9.00

$$t = \frac{tv}{15-v} + \frac{tv}{15+v} \quad /: t > 5$$

$$(15-v)(15+v) = v(15+v) + v(15-v)$$

$$225 - v^2 = 15v + v^2 + 15v - v^2$$

$$v^2 + 30v - 225 = 0$$

$$v_{1,2} = \frac{-30 \pm \sqrt{1800}}{2}$$

$$v = 6.213 \quad (v > 0)$$

.5(15-6.213) = " 43.93 : B - , " 6.213
 . 43.93/6.213 = 7.07 ,
 . 9.00 , A 9.00 12.07 ,
 .(9.04)
 . 9.00 :

$-1 < q < 1$, a_1, a_2, a_3, \dots - .

$a_1 q = 6(1 - q) :$ $\frac{a_2}{1 - q} = 6 :$, 6

a_n^*
 $\frac{a_{n+1}^*}{a_n^*} = -\frac{a_{n+1}}{a_n} = -q$

$-a_1 q = -3(1 + q) :$ $\frac{-a_2}{1 + q} = -3 :$, -3

$-1 = \frac{-2(1 - q)}{1 + q} :$

:

$-1 = \frac{-2(1 - q)}{1 + q}$

$-1 - q = -2 + 2q$

$1 = 3q$

$q = \frac{1}{3}$

$a_1 \cdot \frac{1}{3} = 6(1 - \frac{1}{3}) \rightarrow a_1 = 12$

$\frac{1}{a_2}, \frac{1}{a_3}, \frac{1}{a_4}, \dots :$

$(n -)$

$\frac{a_{n+1}^*}{a_n^*} = \frac{\frac{1}{a_{n+1}}}{\frac{1}{a_n}} = \frac{a_n}{a_{n+1}} = \frac{1}{q} = 3$

(3)

:

$$\cdot 273.25$$

$$\cdot 0.25$$

$$n \cdot$$

$$a_2 = a_1 q = 12 \cdot \frac{1}{3} = 4$$

$$273.25 = \frac{0.25(3^n - 1)}{3 - 1}$$

$$2187 = 3^n$$

$$\boxed{n = 7}$$

$$\cdot n = 7 :$$

- \bar{A}
- \bar{B}
- A
- B

$$P(A \cap B) = P(A) \cdot P(B) \quad P(A/B) = P(A) \quad , P(B/A) = P(B) \quad : \quad : \quad \text{B - A}$$

$$P(A) = 2P(B)$$

$$P(A/B) = 0.6 \rightarrow P(A) = 0.6 \rightarrow P(B) = 0.3$$

$$P(A \cap B) = P(A) \cdot P(B) = 0.6 \cdot 0.3 = 0.18$$

18% :

$$6 - 2$$

$$P(B/A) = P(B) = 0.3$$

$$1 \quad 0 -$$

$$. 0.7^6 \quad 0 -$$

$$6 \quad 1$$

$$. k = 1 , p = 0.3 , n = 6 \quad ,$$

$$P_6(1) = \binom{6}{1} (0.3)^1 (1-0.3)^{6-1}$$

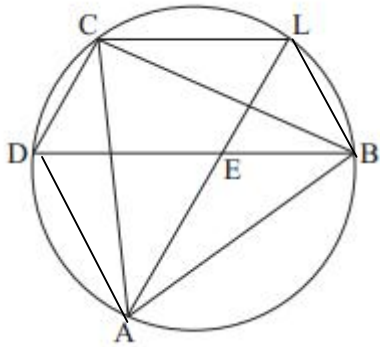
$$P_6(1) = \frac{6!}{1!(6-1)!} \cdot 0.3^1 \cdot 0.7^5$$

$$P_6(1) = 6 \cdot 0.3^1 \cdot 0.7^5$$

$$P_6(1) = 0.302526$$

$$1 - (0.7^6 + 0.302526) = 0.579825 :$$

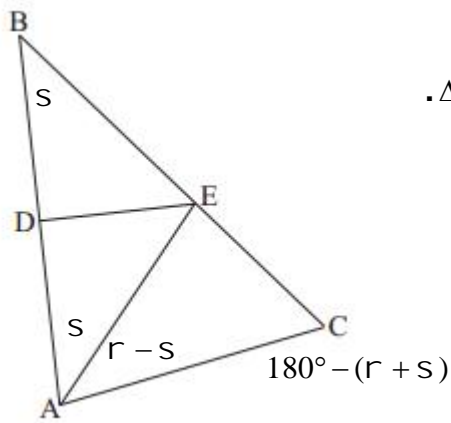
$$. 0.579825 \quad :$$



BD || LC .2 ΔABC .1
 ΔADE (1) LEDC . : "
 LC + LB = LA (2)

	ΔABC	3	1
60° -	∠CAB = ∠CBA = 60°	4	4
	∠CDB = ∠CLA = 60°	5	4
	BD LC	6	2
180° -	∠LCD = ∠LED = 120°	7	6,5
	LEDC	8	7,5
. . .			
60° -	∠BCA = 60°	9	4
	∠BDA = 60°	10	9
180° -	∠DEA = 60°	11	7
ΔADE 180°	∠DAE = 60°	12	10,11
ΔADE	ΔADE	13	12,11,10
(1) . . .			
	LE + EA = LA	14	
	DE = EA	15	13
	LC = DE	16	8
	LC = EA	17	16,15
	∠LCB = ∠CBD	18	6
	LB = CD	19	18
	LE = CD	20	8
	LE = LB	21	20,19
	LC + LB = LA	22	21,17,14
(2) . . .			

. ΔABE -
 .() $\angle EAC = r - s$ - $\angle BAE = s$



.(ΔABC - 180°)
 . ΔAEC -

() $\angle ABC = s$, $\angle BCD = r$ (1) .

AB - DE
 ΔABE -

. $\angle EAC = r - s$:

$$\frac{CE}{EB} \quad (2)$$

() $\angle BCA = 180^\circ - (r + s)$

$$\frac{CE}{AE}$$

$$\frac{CE}{\sin(r - s)} = \frac{EA}{\sin(180^\circ - (r + s))}$$

$$\frac{CE}{EA} = \frac{\sin(r - s)}{\sin(r + s)}$$

EB = EA -

$$\frac{CE}{EB} = \frac{\sin(r - s)}{\sin(r + s)} ;$$

$\therefore s = r - s$ BAC AE :
 $(\Delta ABC - 180^\circ) \angle BCA = 60^\circ - r = 80^\circ, s = 40^\circ$
 $(\Delta ATC - 180^\circ) \angle ATC = 110^\circ - \angle TCA = 30^\circ : BCA$ CT
 $, \Delta ABC - T, AC$ TZ
 $. Z$ AC

$$. () AC = " 10$$

$\Delta ATC - AT$

$$\frac{AT}{\sin 30^\circ} = \frac{AC}{\sin 110^\circ}$$

$$AT = \frac{10 \sin 30^\circ}{\sin 110^\circ}$$

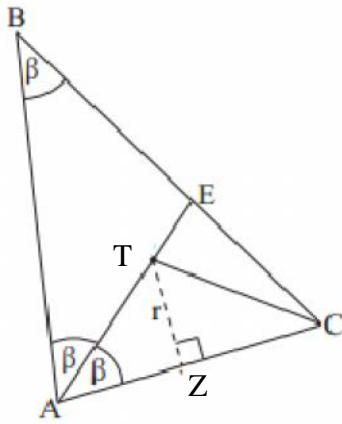
$$\boxed{AT = 5.321cm}$$

$\Delta ATZ - TZ$

$$\sin 40^\circ = \frac{TZ}{AT}$$

$$5.321 \sin 40^\circ = TZ$$

$$\boxed{TZ = 3.42cm}$$



. " 3.42 ABC :

.() A

,AF

A

.(

.(180°) ∠BCA = 90° - (r + s) - (

.(

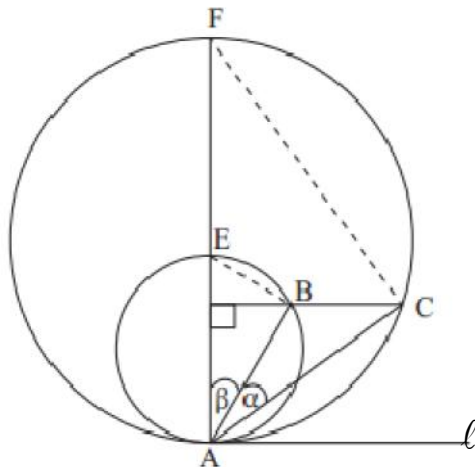
.ΔCAB -

. ∠FCA = ∠EBA = 90°

ΔABE

$$\frac{AB}{\sin(90^\circ - s)} = 2r$$

$$\boxed{AB = 2r \cos s}$$



.() ∠FAB = s , ∠BAC = r (1) .

EA - ,

FEA

ℓ

ℓ

FEA

) CB ⊥ AF () BC ∥ ℓ

. ∠BCA = 90° - (r + s) :

$$\frac{AC}{AB} \quad (2)$$

) ∠CBA = 90° + s

$$\frac{AC}{AB}$$

$$\frac{AC}{\sin(90^\circ + s)} = \frac{AB}{\sin(90^\circ - (r + s))}$$

$$\boxed{\frac{AC}{AB} = \frac{\cos s}{\cos(r + s)}}$$

$$\frac{AC}{AB} = \frac{\cos s}{\cos(r + s)} :$$

AE = 2r ,

AF = 2R .

ΔAFC

$$\frac{AC}{\sin(90^\circ - (r + s))} = 2R$$

$$\boxed{AC = 2R \cos(r + s)}$$

$$\frac{AC}{AB} = \frac{2R \cos(r + s)}{2r \cos s}$$

$$\frac{\cos s}{\cos(r + s)} = \frac{R \cos(r + s)}{r \cos s}$$

$$\boxed{\frac{R}{r} = \frac{\cos^2 s}{\cos^2(r + s)}}$$

$$\frac{R}{r} = \frac{\cos^2 s}{\cos^2(r + s)} :$$

x , $a > 1$, $f(x) = \frac{x^2 + x - a}{x^2 - x + a}$:

$$f(x) \tag{1}$$

$y = 1$, $\lim_{x \rightarrow \pm\infty} \frac{x^2 + x - a}{x^2 - x + a} = \lim_{x \rightarrow \pm\infty} \frac{\frac{x^2}{x^2} + \frac{x}{x^2} - \frac{a}{x^2}}{\frac{x^2}{x^2} - \frac{x}{x^2} + \frac{a}{x^2}} = \lim_{x \rightarrow \pm\infty} \frac{1+0-0}{1-0+0} = 1$

$y = 1$:

$$\tag{2}$$

$$f'(x) = \frac{(2x+1)(x^2 - x + a) - (2x-1)(x^2 + x - a)}{(x^2 - x + a)^2}$$

$$f'(x) = \frac{2x^3 - 2x^2 + 2ax + x^2 - x + a - (2x^3 + 2x^2 - 2ax - x^2 - x + a)}{(x^2 - x + a)^2}$$

$$f'(x) = \frac{2x^3 - 2x^2 + 2ax + x^2 - x + a - 2x^3 - 2x^2 + 2ax + x^2 + x - a}{(x^2 - x + a)^2}$$

$$f'(x) = \frac{-2x^2 + 4ax}{(x^2 - x + a)^2}$$

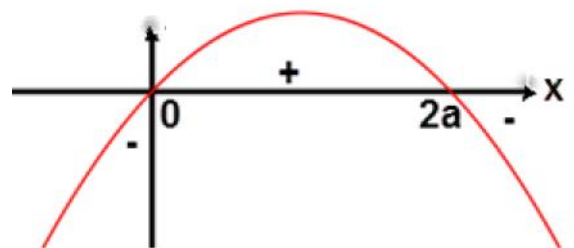
$$0 = -2x^2 + 4ax$$

$$0 = 2x(-x + 2a)$$

$$x = 0 \rightarrow (0, -1)$$

$$x = 2a \rightarrow y = \frac{4a^2 + 2a - a}{4a^2 - 2a + a} \quad /:(a > 1) \rightarrow (2a, \frac{4a+1}{4a-1})$$

()



$x = 0$ -

$x = 2a$ -

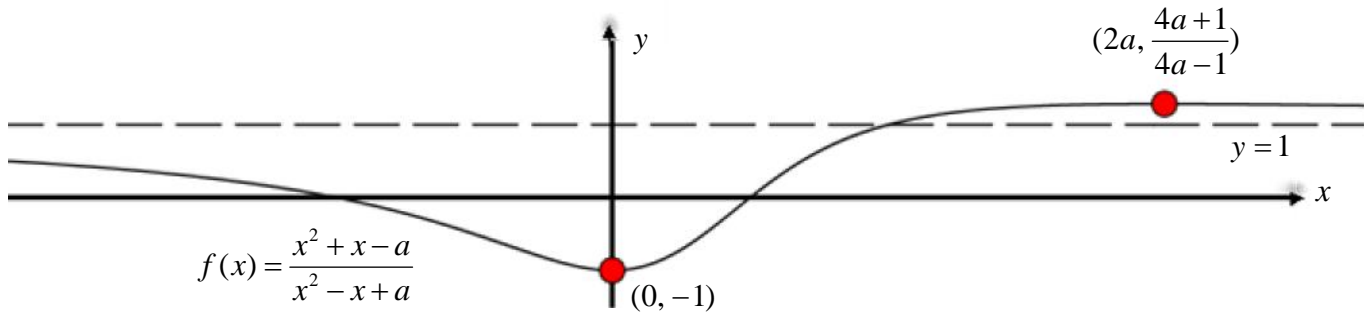
$$(2a, \frac{4a+1}{4a-1}) , (0, -1) :$$

"

x -

,

(3)



$$f(x) = \frac{x^2 + x - a}{x^2 - x + a}$$

, $x < 0$

,

, $x < 0$

,

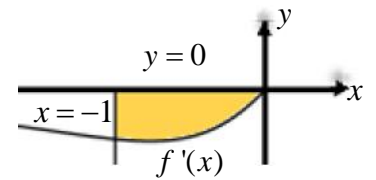
.

:(2)

0

$x \leq 0$

$$\cdot \frac{1}{2} -$$



$$S = \int_{-1}^0 (0 - f'(x)) dx = -f(x) \Big|_{-1}^0 = -f(0) + f(-1) = -(-1) + \frac{1-1-a}{1+1+a} = 1 - \frac{a}{2+a}$$

$$\frac{1}{2} = 1 - \frac{a}{2+a}$$

$$\frac{a}{2+a} = \frac{1}{2}$$

$$2a = 2+a$$

$$\boxed{a = 2}$$

$$\cdot f(x) = \frac{x^2 + x - 2}{x^2 - x + 2}$$

$$\cdot x^2 + x - 2 = 0 \quad f(x) = 0 \quad x -$$

$$\cdot x = -2, 1 \quad (x+2)(x-1) = 0$$

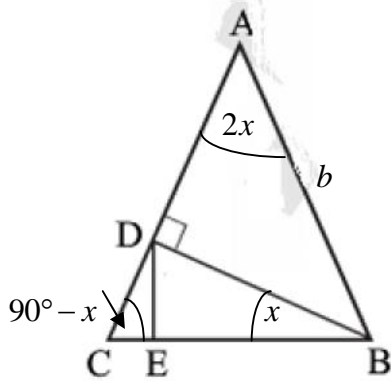
$$\cdot (-2, 0) - (1, 0) \quad x - \quad :$$

מקסימום אורך האנך DE

$\angle C = \frac{180^\circ - 2x}{2} = 90^\circ - x$: , $\triangle ABC$

(, , ,)

$\angle DBE = x$, $\triangle DBC$



$\triangle BDE$

$\triangle ABD$

$\sin x = \frac{DE}{BD}$

$\sin 2x = \frac{BD}{AB}$

$b \sin 2x \sin x = DE$

$b \sin 2x = BD$

$\triangle BDE$

$\triangle BCD$

$\sin x = \frac{DE}{BD}$

$\sin(180^\circ - 2x) = \frac{BD}{AB}$

$b \sin 2x \sin x = DE$

$b \sin 2x = BD$

$DE(x) = b \sin 2x \sin x$:

$(DE)'(x) = b(2 \cos 2x \sin x + \sin 2x \cos x)$

$(DE)'(x) = b(2 \cos 2x \sin x + 2 \sin x \cos x \cos x)$

$(DE)'(x) = 2b \sin x (\cos 2x + \cos^2 x)$

~~$0 = \sin x$~~ $\leftarrow 0 < x < \frac{f}{2}$

$\cos 2x + \cos^2 x = 0$

$2 \cos^2 x - 1 + \cos^2 x = 0$

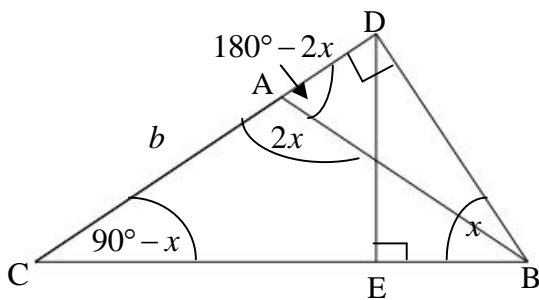
$\cos^2 x = \frac{1}{3}$

$\cos x = \pm \sqrt{\frac{1}{3}}$

$\cos x = -\sqrt{\frac{1}{3}} \rightarrow x = 2.186 + 2fk \leftarrow 0 < x < \frac{f}{2}$

$\cos x = \sqrt{\frac{1}{3}} \rightarrow x = 0.955 + 2fk \rightarrow x = 0.955 \leftarrow 0 < x < \frac{f}{2}$

$f'(0.9) = 0.25b > 0$
 $f'(1) = -0.21b < 0$ } max



$$, x = 0.955$$

DE -

$$. x = \frac{0.955}{f} \cdot 180^\circ = 54.72^\circ$$

$$\sphericalangle \text{BAC} = 2x = 2 \cdot 54.72^\circ$$

$$\boxed{\sphericalangle \text{BAC} = 109.43^\circ}$$

· , ,

· DE , $\sphericalangle \text{BAC} = 109.43^\circ$:

$1 < x < 2$

$f(x)$

x	1.1	1.2	1.3	1.4
f(x)	1.19	1.28	1.36	1.43

$1 < x < 2$

$f(x)$

.(

$f'(1.3) < f'(1.2) < f'(1.1)$

$f'(1.2)$

$f''(x)$

$f'(x)$

$1 < x < 2$

$g(x) = \sqrt{f(x)}$

$g(x) = \sqrt{f(x)}$

$f(x)$

.(

$f(x)$

$f'(x)$

$g'(x) = \frac{f'(x)}{2\sqrt{f(x)}}$

$g(x)$

. x

$1 < x < 2$

$1.1 \leq x \leq 1.3$

$g'(x) = f'(x)$

$\frac{f'(x)}{2\sqrt{f(x)}} = f'(x) \quad \because f'(x) > 0$

$\frac{1}{2\sqrt{f(x)}} = 1$

$\frac{1}{2} = \sqrt{f(x)}$

$\frac{1}{4} = f(x)$

,

1.19

$1.1 \leq x \leq 1.3$

$f(x)$

$1.1 \leq x \leq 1.3$

$\frac{1}{4} = f(x)$

. :

"